

# Exponential Functions Review Sheet

## SIMPLIFYING EXPONENTIAL EXPRESSIONS

Use properties of exponents to simplify each expression.

$$1. (2a^2)^3$$

$$2^3 a^{2 \cdot 3}$$

$$\boxed{8a^6}$$

$$2. 2x^4z \cdot 3z^4x^3$$

$$2 \cdot 3 \cdot x^4 x^3 \cdot z z^4$$

$$6x^{4+3} z^{1+4}$$

$$\boxed{6x^7 z^5}$$

$$3. [(p^3)^3]^2$$

$$p^{3 \cdot 3 \cdot 2} = \boxed{p^{18}}$$

$$4. \frac{x^6}{x^8} = x^{6-8} = x^{-2}$$

$$= \boxed{\frac{1}{x^2}}$$

$$5. \frac{b^0 c^{-2}}{a^{-5}} = \frac{c^{-2}}{a^{-5}} = \boxed{\frac{a^5}{c^2}}$$

$$6. \left(\frac{8x^3}{y}\right)^2$$

$$= \frac{8^2 x^{3 \cdot 2}}{y^2} = \boxed{\frac{64 x^6}{y^2}}$$

## RATIONAL EXPONENTS

Convert any radicals to exponential form, and express rational exponents in radical form.

$$7. \sqrt[5]{wy^3} = (wy)^{3/5}$$

$$\left[ \begin{array}{l} \text{num.} = 3 \\ \text{denom.} = 5 \end{array} \right]$$

$$8. mp^{\frac{2}{7}}$$

index: 7  
power: 2

$$\boxed{m \sqrt[7]{p^2}}$$

$$9. 4\sqrt[4]{bd^9}$$

num: 9  
denom: 4

$$\boxed{4(bd)^{9/4}}$$

Solve the given equations for x.

$$10. 6^{x+3} = 6^5$$

$$x+3=5$$

$$\boxed{x=2}$$

$$11. 3^{5x-3} = 3^{4x+7}$$

$$5x-3 = 4x+7$$

$$5x-4x = 7+3$$

$$\boxed{x=10}$$

## SCIENTIFIC NOTATION

Express each number in scientific notation.

$$12. 980,200,000,000,000$$

$$9.802 \times 10^{14}$$

$$13. 0.000000000008$$

$$8 \times 10^{-11}$$

Express each number in standard form.

$$14. 1.86 \times 10^{-4}$$

$$.000186$$

$$15. 4.9 \times 10^5$$

$$490,000$$

Simplify. Show your work. Final answers should be written in scientific notation.

16.  $(8.8 \times 10^8)(3.5 \times 10^{-13})$

$$8.8 \cdot 3.5 \times 10^{8+(-13)}$$

$$30.8 \times 10^{-5}$$

$$\boxed{3.08 \times 10^{-4}}$$

17.  $(1.35 \times 10^8)(7.2 \times 10^{-4})$

$$1.35 \cdot 7.2 \times 10^{8+(-4)}$$

$$\boxed{9.72 \times 10^8}$$

18.  $\frac{(2.376 \times 10^{-4})}{(7.2 \times 10^{-8})}$

$$\div .33 \times 10^{-4-(-8)}$$

$$.33 \times 10^4$$

$$\boxed{3.3 \times 10^3}$$

19.  $\frac{(8.74 \times 10^{-3})}{(1.9 \times 10^5)}$

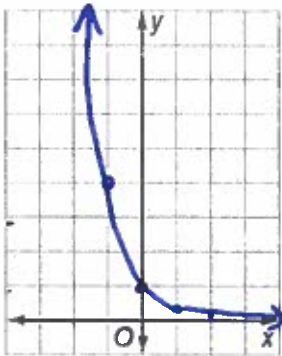
$$\div 4.6 \times 10^{-3-5}$$

$$\boxed{4.6 \times 10^{-8}}$$

### EXPONENTIAL FUNCTIONS

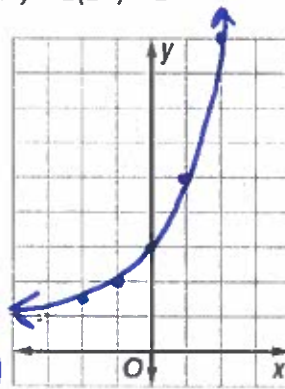
Graph the given exponential functions using a table.

20.  $y = \left(\frac{1}{4}\right)^x$



x	$\left(\frac{1}{4}\right)^x$	y	(x, y)
-2	$\left(\frac{1}{4}\right)^{-2}$	16	(-2, 16)
-1	$\left(\frac{1}{4}\right)^{-1}$	4	(-1, 4)
0	$\left(\frac{1}{4}\right)^0$	1	(0, 1)
1	$\left(\frac{1}{4}\right)^1$	1/4	(1, 1/4)
2	$\left(\frac{1}{4}\right)^2$	1/16	(2, 1/16)

21.  $y = 2(2^x) + 1$



x	$2(2^x) + 1$	y
-2	$2(2^{-2}) + 1 = 2(1/4) + 1$	1.5
-1	$2(2^{-1}) + 1 = 2(1/2) + 1$	2
0	$2(2^0) + 1 = 2(1) + 1$	3
1	$2(2^1) + 1 = 2(2) + 1$	5
2	$2(2^2) + 1 = 2(4) + 1$	9

Determine whether the set of data shown below displays exponential behavior. Write yes or no. If yes, name the common factor.

22.

x	2	5	8	11
y	480	120	30	7.5

$$\frac{120}{480} = \frac{1}{4} \quad \frac{30}{120} = \frac{1}{4} \quad \frac{7.5}{30} = \frac{1}{4}$$

yes; common factor =  $\frac{1}{4}$

23.

x	21	18	15	12
y	30	23	16	9

$$\frac{30}{23} = 1.30 \quad \frac{23}{16} = 1.44 \dots$$

NO