

WARM-UP

1. How do you decide whether to use **addition** or **subtraction** when solving using elimination?

2. Solve.

$$8x + 5y = 38$$

(+)

$$-8x + 2y = 4$$

$$\cancel{0x} + 7y = 42$$

$$\cancel{7y} = \frac{42}{7}$$

$$y = 6$$

$$8x + 5(\cancel{6}) = 38$$

$$\cancel{8x} + \cancel{30} = 38$$

$$\cancel{8x} = 8$$

$$x = 1$$

(1, 6)

matching coeff., opposite signs.
matching coeff., same sign.

$$\textcircled{6} \quad x + 4y = -8$$

$$x - 4y = -8$$

$$4y - 4y$$

$$4y + 4y = 8y$$

ADD

$$\begin{array}{r} x + 4y = -8 \\ \textcircled{+} x - 4y = -8 \\ \hline 2x + 0y = -16 \\ 2x = -16 \\ \hline x = -8 \end{array}$$

SUBTRACT

$$\begin{array}{r} x + 4y = -8 \\ \textcircled{-} x - 4y = -8 \\ \hline \textcircled{0}x + 8y = 0 \\ 8y = 0 \\ \hline y = 0 \end{array}$$

$$(-8, 0)$$

~~8, 5, 6, 9, 8, 7~~

③ $x + 4y = 11$

$\ominus x - 6y = 11$

$\ominus x + 10y = 0$

$\frac{10y}{10} = \frac{0}{10}$

$y = 0$

$x + 4(0) = 11$

$x + 0 = 11$

$x = 11$

$4y - -6y =$

$4y + 6y = 10y$

$(11, 0)$

x, y

⑤ $3x + 4y = 19$

$\ominus 3x + 6y = 33$

$\ominus x - 2y = -14$

$\frac{-2y}{-2} = \frac{-14}{-2}$

$y = 7$

$3x + 4(7) = 19$

$3x + 28 = 19$

$-28 -28$

$3x = -9$

$x = -3$

$(-3, 7)$

⑧ $3x - y = -1$

$-3x - y = 5$

ADD

$\oplus \begin{array}{r} 3x - y = -1 \\ -3x - y = 5 \\ \hline \end{array}$

$\ominus x - 2y = 4$

$\frac{-2y}{-2} = \frac{4}{-2}$

$y = -2$

SUBTRACT

$\ominus \begin{array}{r} 3x - y = -1 \\ -3x - y = 5 \\ \hline \end{array}$

$6x + 0y = -6$

$\frac{6x}{6} = \frac{-6}{6}$

$x = -1$

$(-1, 2)$

⑨ $2x - 3y = 9$

$\ominus -5x - 3y = 30$

$7x + 0y = -21$

$\frac{7x}{7} = \frac{-21}{7}$

$x = -3$

$2(-3) - 3y = 9$

$-6 - 3y = 9$

$\frac{-3y}{-3} = \frac{15}{-3}$

$y = -5$

$(-3, -5)$

8, 3, 2, 10

$$\begin{aligned} \textcircled{2} \quad -x + y &= 1 \\ x + y &= 11 \end{aligned}$$

$$\begin{array}{r} \text{ADD} \\ \hline \cancel{-x + y = 1} \\ \oplus \quad \cancel{x + y = 11} \\ \hline \cancel{0x + 2y = 12} \end{array}$$

$$\begin{array}{r} \cancel{2y} = 12 \\ \hline 2 \quad 2 \\ \hline y = 6 \end{array}$$

$$\begin{array}{r} x + y = 11 \\ \quad -6 \\ \hline x = 5 \end{array}$$

(5, 6)

$$\begin{array}{r} \text{SUB} \\ \hline -x + y = 1 \\ \ominus \quad x + y = 11 \\ \hline -2x + 0y = -10 \end{array}$$

$$\begin{aligned} \textcircled{5} \quad x + 4y &= 11 \\ \Rightarrow x - 6y &= 11 \\ \hline \cancel{0x + 10y} &= 0 \\ 10 \quad 10 \\ \hline y &= 0 \end{aligned}$$

$$\begin{array}{r} x + 4(0) = 11 \\ x = 11 \\ (11, 0) \end{array}$$

$$\begin{aligned} \textcircled{8} \quad 3x - y &= 1 \\ \oplus \quad -3x - y &= 5 \\ \hline \cancel{0x} - 2y &= 4 \\ -2y &= 4 \\ \hline -2 \quad -2 \\ \hline y &= -2 \end{aligned}$$

$$\begin{array}{r} 3x - (-2) = -1 \\ 3x + 2 = -1 \\ \hline 3x = -3 \\ \hline x = -1 \end{array}$$

(-1, -2)

$$\begin{aligned} \textcircled{10} \quad x - y &= 4 \\ \oplus \quad 2x + y &= -4 \\ \hline 3x + 0y &= 0 \\ \hline 3x &= 0 \\ \hline x &= 0 \end{aligned}$$

$$\begin{array}{r} 0 - y = 4 \\ -y = 4 \\ \hline y = -4 \end{array}$$

(0, -4)