

## Substitution

Use substitution to solve each system of equations. When necessary, solve one equation in the system for a variable first. Be sure to show all work and box/circle your final answer.

$$1. \begin{cases} y = 4x \\ x + y = 5 \end{cases}$$

$$x + 4x = 5$$

$$\frac{5x}{5} = \frac{5}{5}$$

$$x = 1$$

$$y = 4(1) = 4$$

$$\boxed{(1, 4)}$$

$$2. \begin{cases} y = 2x \\ x + 3y = -14 \end{cases}$$

$$x + 3(2x) = -14$$

$$x + 6x = -14$$

$$7x = -14$$

$$x = -2$$

$$y = 2(-2) = -4$$

$$\boxed{(-2, -4)}$$

$$3. \begin{cases} y = 3x \\ 2x + y = 15 \end{cases}$$

$$2x + (3x) = 15$$

$$5x = 15$$

$$x = 3$$

$$y = 3(3) = 9$$

$$\boxed{(3, 9)}$$

$$4. \begin{cases} x = -4y \\ 3x + 2y = 20 \end{cases}$$

$$3(-4y) + 2y = 20$$

$$-12y + 2y = 20$$

$$-10y = 20$$

$$y = -2$$

$$x = -4(-2) = 8$$

$$\boxed{(8, -2)}$$

$$5. \begin{cases} y = x - 1 \\ x + y = 3 \end{cases}$$

$$x + (x - 1) = 3$$

$$x + x - 1 = 3$$

$$2x - 1 = 3$$

$$2x = 4$$

$$\boxed{x = 2}$$

$$2 + y = 3$$

$$y = 1$$

$$\boxed{(2, 1)}$$

$$6. \begin{cases} x = y - 7 \\ x + 8y = 2 \end{cases}$$

$$(y - 7) + 8y = 2 \quad x = 1 - 7$$

$$y - 7 + 8y = 2 \quad x = -6$$

$$9y - 7 = 2$$

$$9y = 9$$

$$y = 1$$

$$\boxed{(-6, 1)}$$

$$7. \begin{cases} y = 4x - 1 \\ y = 2x - 5 \end{cases}$$

$$4x - 1 = 2x - 5$$

$$2x - 1 = -5$$

$$2x = -4$$

$$x = -2$$

$$y = 4(-2) - 1 = -9$$

$$\boxed{(-2, -9)}$$

$$8. \begin{cases} y = 3x + 8 \\ 5x + 2y = 5 \end{cases}$$

$$5x + 2(3x + 8) = 5$$

$$5x + 6x + 16 = 5$$

$$11x + 16 = 5$$

$$11x = -11$$

$$x = -1$$

$$y = 3(-1) + 8 = 5$$

$$\boxed{(-1, 5)}$$

$$9. \begin{cases} 2x - 3y = 21 \\ y = 3 - x \end{cases}$$

$$2x - 3(3 - x) = 21$$

$$2x - 9 + 3x = 21$$

$$5x - 9 = 21$$

$$5x = 30$$

$$x = 6$$

$$y = 3 - 6 = -3$$

$$\boxed{(6, -3)}$$

$$10. \begin{cases} y = 5x - 8 \\ 4x + 3y = 33 \end{cases}$$

$$4x + 3(5x - 8) = 33$$

$$4x + 15x - 24 = 33$$

$$19x - 24 = 33$$

$$19x = 57$$

$$x = 3$$

$$y = 5(3) - 8 = 7$$

$$\boxed{(3, 7)}$$

$$11. \begin{cases} x + 2y = 13 \\ 3x - 5y = 6 \end{cases} \rightarrow x = -2y + 13$$

$$3(-2y + 13) - 5y = 6$$

$$-6y + 39 - 5y = 6$$

$$-11y + 39 = 6$$

$$-11y = -33$$

$$y = 3$$

$$x = -2(3) + 13 = 7$$

$$\boxed{(3, 7)}$$

$$12. \begin{cases} x + 5y = 4 \\ 3x + 15y = -1 \end{cases} \rightarrow x = -5y + 4$$

$$3(-5y + 4) + 15y = -1$$

$$-15y + 12 + 15y = -1$$

$$12 = -1$$

$\boxed{\text{NO SOLUTION}}$

$$13. \begin{cases} 3x - y = 4 \\ 2x - 3y = -9 \end{cases} \rightarrow -y = -3x + 4$$

$$y = 3x - 4$$

$$2x - 3(3x - 4) = -9$$

$$2x - 9x + 12 = -9$$

$$-7x + 12 = -9$$

$$-7x = -21$$

$$x = 3$$

$$y = 3(3) - 4 = 5$$

$$\boxed{(3, 5)}$$

$$14. \begin{cases} x + 4y = 8 \\ 2x - 5y = 29 \end{cases} \rightarrow x = -4y + 8$$

$$2(-4y + 8) - 5y = 29$$

$$-8y + 16 - 5y = 29$$

$$-13y + 16 = 29$$

$$-13y = 13$$

$$y = -1$$

$$x = -4(-1) + 8 = 12$$

$$\boxed{(12, -1)}$$

$$15. \begin{cases} x - 5y = 10 \\ 2x - 10y = 20 \end{cases} \rightarrow x = 5y + 10$$

$$2(5y + 10) - 10y = 20$$

$$10y + 20 - 10y = 20$$

$$20 = 20$$

$\boxed{\text{infinite}}$